## Unboxing ARX-based White-Box Ciphers: Chosen-Plaintext Computation Analysis and Its Applications

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## Outline

1. ARX-Based White-Box Ciphers
2. Computation Analysis against White-Box SPECK
3. Chosen-Plaintext Computation Analysis
4. Attack Instances of CP-DCA and CP-ADCA
5. Conclusion

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## White-Box Cryptography

- Goal: prevents the cryptographic algorithm from the key extraction in white-box context.
- Technique: applies the encoding to hide the sensitive information.
- Framework:
- CEJO (SAC'02): a network of look-up tables (LUTs) with linear/non-linear encodings.
- Self-equivalence (SAC'20): hides the key in the affine layer with self-equivalence encodings.
- Implicit function (CRYPTO'22): hides the key in the binary multivariate polynomials with self-equivalence and linear/non-linear encodings.


## LUTs in CEJO Framework

- At SAC 2002, Chow et al. proposed the CEJO framework.
- It transforms the round function into a series of look-up tables (LUTs) with embedded secret key and applies linear/non-linear encodings to protect the LUTs.


Figure: Type II: key-dependent T-boxes/Tyi table


Figure: Type III: compatibility of encodings between consecutive rounds


Figure: Type IV: encoded nibble XOR table

## Self-Equivalence Encodings

- At SAC 2020, Ranea and Preneel proposed the self-equivalence framework.


## Definition

(Self-equivalence). Let $F$ be an $n$-bit function. A pair of $n$-bit affine permutations $(A, B)$ such that $F=B \circ F \circ A$ is called an (affine) self-equivalence of $F$.

- Self-equivalence of Sbox: $S=B \circ S \circ A$.
- Round function: $E=L \circ S \circ \oplus k$.



## Self-Equivalence White-Box Implementation

- Let $A L^{r}=A \circ \oplus k^{r} \circ L \circ B$.
- Round functions:

$$
\begin{gathered}
\bar{E}_{k^{n}}^{n} \circ \cdots \circ \bar{E}_{k^{1}}^{1}=(L \circ B) \circ S \circ\left(A \circ \oplus k^{n} \circ L \circ B\right) \circ S \circ \cdots \circ S \circ\left(A \circ \oplus k^{1}\right) \\
=(L \circ B) \circ S \circ A L^{n} \circ S \circ \cdots \circ S \circ A L^{2} \circ S \circ\left(A \circ \oplus k^{1}\right) .
\end{gathered}
$$

- Introducing the external encodings $P$ and $Q$ such that:

$$
A L^{n+1}=Q \circ L \circ B, A L^{1}=A \circ \oplus k^{1} \circ P
$$

- Encoded encryption: $\bar{E}_{k}=A L^{n+1} \circ S \circ \cdots \circ S \circ A L^{1}$
$\Rightarrow$ consists of the affine function $A L$ and the substitution $S$.


## Algebraic Attacks against CEJO and Self-Equivalence

- CEJO:
- SASAS $\Rightarrow$ ASA $\Rightarrow$ affine equivalence problems.
- CEJO-WBAES: time complexity $2^{22}$, XL-WBAES: time complexity $2^{32}$.
- Self-Equivalence:
- Sparse matrix.
- Diagonal encodings.
- A few pairs of self-equivalences: 2040 of AES and SM4 Sbox.
- Both frameworks apply small encodings to protect a small SBox.
- New direction: large substitution layer with many pairs of self-equivalences and large dimension of encodings.


## Self-Equivalence White-Box SPECK

At ACNS 2022, Vandersmissen et al. proposed a self-equivalence white-box SPECK (SE-SPECK) implementations.

- Transforming the ARX to SPN:

$$
E_{k}=\left(A L^{\left(n_{r}\right)} \circ S\right) \circ \cdots \circ\left(A L^{(1)} \circ S\right) \circ A L^{(0)} .
$$



## Self-Equivalence White-Box SPECK

- Let $\overline{A L^{(r)}}=A \circ A L^{(r)} \circ B, S=B \circ S \circ A$,

$$
\begin{aligned}
& E_{k}^{\prime}=\left(A L^{(n)} \circ B\right) \circ S \circ\left(A \circ A L^{(r)} \circ B\right) \circ S \circ \cdots \circ S \circ A L^{(0)} \\
& =\left(A L^{(n)} \circ B\right) \circ S \circ \overline{A L^{(n)}} \circ S \circ \cdots \circ S \circ \overline{A L^{(1)}} \circ S \circ A L^{(0)} .
\end{aligned}
$$

- External encodings:
- For some random bijections I and $O$ :
- $\overline{A L^{(0)}}=A L^{(0)}$ 。 .
- $\overline{A L^{(n)}}=O \circ A L^{(n)} \circ B$.


## Algebraic Attacks against SE-SPECK

- The key is embedded in the affine layer $A L^{r}=A \circ \oplus k^{r} \circ L \circ B$.
- The self-equivalences $A$ and $B$ has the sparse matrices with $2 n+11$ variable entries.
- The key can be recovered by constructing a system of linear equations based on a few of unknown variables.


## Implicit Framework to ARX Ciphers

At CRYPTO 2022, Ranea et al. proposed an implicit framework to ARX Ciphers.

- Representing each round function by a low-degree implicit function (efficient implementation).
- Encoding the implicit function with large affine permutations and even large non-linear self-equivalences.
- Combining the large self-eqivalences with large affine encodings (hide the sparse matrix).


## Implicit Framework to ARX Ciphers

## Definition

(Implicit function). Let $F$ be an $n$-bit function. A $(2 n, m)$-bit function $P$ is called an implicit function of $F$ if it satisfies $P(x, y)=0 \Leftrightarrow y=F(x)$.

- $I, O \leftarrow$ round encodings, $T \leftarrow$ implicit function of $S, U \leftarrow\left(B^{-1}, A\right)$ such that $S=B \circ S \circ A, V \leftarrow$ a random linear transformation.

- Implicit round function $\Rightarrow$ linear system:

$$
\begin{gathered}
P(x, y)=V \circ T \circ\left(\left(A \circ \oplus k \circ I(x), B^{-1} \circ L^{-1} \circ O^{-1}(y)\right)\right)=0 \\
\Leftrightarrow \underline{V \circ B^{-1} \circ L^{-1} \circ O^{-1}}(y)=\underline{V \circ S \circ A \circ \oplus k \circ I(x)}
\end{gathered}
$$

## Implicit Framework to ARX Ciphers

- Let $E=L \circ S \circ \oplus k$, without the representation of an implicit function:

$$
\overline{E^{(i)}}=C^{(i+1)} \circ E^{(i)} \circ A^{(i)} \circ B^{(i-1)} \circ\left(C^{(i)}\right)^{-1}
$$

where

$$
E^{(i)}=B^{(i)} \circ E^{(i)} \circ A^{(i)} .
$$

- The canceling rule of the implicit self-equivalence implementation:



## Algebraic Attacks against Implicit Framework

- The key is embedded in the implicit round function:

$$
\overline{E^{(i)}}=C^{(i+1)} \circ\left(B^{(i)}\right)^{-1} \circ E_{k}^{(i)} \circ B^{(i-1)} \circ\left(C^{(i)}\right)^{-1} .
$$

- The quadratic self-equivalences $B$ is extremely sparse with a few monomials, up to affine equivalence.
- The key recovery on the structure $A S A$ with modular addition $S$.
- Time complexity $\mathcal{O}\left(n^{9}\right) / \mathcal{O}\left(n^{6}\right)$ with/without external encodings [BLU23].


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## Differential Computation Analysis

At CHES 2016, differential computation analysis (DCA) was proposed to perform a statistical analysis on the computation traces of white-box implementations.

## - Noise-Free Computation Traces

The first/last-round computed values (accessed memory/register) by using DBI tools.


- Differential Power Analysis

Dividing the traces in two distinct sets based on key guesses, computing the difference of two sets, distinguishing the correct key with the highest peak.


## Differences between Algebraic Attack and DCA

| Difference | Algebraic Attack | DCA |
| :---: | :---: | :---: |
| Context | white-box | gray-box |
| Process | 1) unpacks the obfuscation layers <br> 2) pinpoints the target function | 1) collects the computation traces |
| 2) decodes the encoded structure |  |  |
| Reverse Engineering | 2) analyzes the traces |  |$\quad$| not required |
| :---: |
| Time Complexity |

## Computation Analysis (CA)

- Following DCA, many other computation analyses are proposed.
- $F=N \circ L \leftarrow$ the internal encoding, $\varphi \leftarrow$ a sensitive function.

| Distinguisher | Attack <br> Context | Method | Analysis of Key Leakage | Time Complexity |
| :---: | :---: | :---: | :---: | :---: |
| DCA [BHMT16] | gray-box | correlation computation | - | $2^{22}$ |
| IDCA [BBB+19] |  |  | $\mathrm{HW}=1$ of $L$ | $2^{27}$ |
| CPA [RW19] |  |  | non-injection of $\varphi$ bijection of $F$ | $2^{22}$ |
| CA [RW19] |  |  |  | $2^{29}$ |
| MIA [RW19] |  |  |  | $2^{22}$ |
| SA [SMG16] |  | spectral <br> analysis | - | $2^{27}$ |
| MSA [LJK20] |  |  | imbalance of $L$ | $2^{22}$ |
| ISA [CGM21] | white-box |  | non-invertibility of $L$ | $2^{32}$ |
| ADCA [TGLZ23] | gray-box | detection of algebraic degree | $d_{a l g}(F) \leq 6$ | $2^{21.32} \sim 2^{24.07}$ |

## Algebraic Degree Computation Analysis

At CHES 2023, Tang et al. proposed the algebraic degree computation analysis (ADCA).

- It can distinguish the correct key by computing the algebraic degrees of target functions.
- ADCA can break the most cases of encodings with the lowest time complexity.
- $k^{*} \leftarrow$ secret key, Target function $O_{k^{*}}=F \circ S \circ \oplus k^{*}$.
- $k \leftarrow$ key guess,

Chosen input $x^{\prime}=\oplus k \circ S^{-1}(x)$.

- If $k=k^{*}, A_{k^{*}}=F$ which is the internal encoding.
- If $k \neq k^{*}, A_{k}=F \circ S \circ \oplus k^{*} \circ \oplus k \circ S^{-1}$ which a random function.



## Analysis of DCA against ARX Structure

- Targeting the first-round key addition.

- Targeting the second-round modular addition.



## Simplified Target Functions

- The first-round key addition.

$$
\begin{aligned}
y & =\left(\left(x_{0}^{(1)} \ggg \alpha\right) \boxplus x_{1}^{(1)}\right) \oplus k \\
\Rightarrow y & =\left(x \boxplus c_{1}\right) \oplus k \\
& =S_{1}(x) \oplus k
\end{aligned}
$$

$$
\begin{aligned}
& y=\left(\left(\left(\left(x_{0}^{(1)} \ggg \alpha\right) \boxplus x_{1}^{(1)}\right) \oplus k\right) \ggg \alpha\right) \boxplus \\
& \quad\left(\left(x_{1} \lll \beta\right) \oplus\left(\left(x_{0}^{(1)} \ggg \alpha\right) \boxplus x_{1}^{(1)}\right) \oplus k\right) \\
& \Rightarrow y=\left(\left(x \boxplus c_{1}\right) \oplus k\right) \boxplus\left(c_{2} \oplus\left(x \boxplus c_{1}\right) \oplus k\right) \\
& \quad=S_{2}\left(S_{1}(x) \oplus k, S_{1}(x) \oplus k \oplus c_{2}\right)
\end{aligned}
$$

- Key addition after substitution.
- Substitution after key addition.


## DCA on SPECK

- Result: For both two target functions, DCA obtains the highest correlation 1 for every key guess and fails to distinguish the correct key.
- Reason:
- The modular addition lacks confusion to fully obfuscate the key information.
- The sensitive values of different key candidates are similar to each other.
- At least one bit of the sensitive values for an incorrect key guess is equal to one bit of the sensitive values corresponding to the correct key.


## Sum-Correlation DCA

- Principal:
- Each bit of the sensitive values for the correct key has correlation 1.
- The correct key has the maximum summed correlations.
- For each key guess, SC-DCA computes the correlation between each bit of the sensitive value $\left(\varphi_{k}(x)\right)_{i}$ and each sample in the traces $\boldsymbol{v}_{j}$.
- It sums the maximum computed correlations of every bit in the sensitive value.
- SC-DCA distinguisher:

$$
\delta_{k}^{\mathrm{SC}-\mathrm{DCA}}=\arg \max \sum_{1 \leq i \leq n} \max _{1 \leq j \leq t}\left|\operatorname{Cor}\left(\left(\varphi_{k}(x)\right)_{i}, \boldsymbol{v}_{j}\right)\right|
$$

## SC-DCA on (White-Box) SPECK

- SC-DCA on SPECK32:
- can successfully distinguish the correct key with the maximum summed correlation 16 .
- Time complexity $2^{38}$ with 4096 traces.
- SC-DCA on white-box SPECK32:
- extracts an incorrect key for both SE-SPECK32 and IF-SPECK32.
- does not consider the encoding phases which obfuscate the sensitive values against DCA.


## Encoded Structure of SE-SPECK

The first three encryption rounds of SE-SPECK without external encodings:


## Encoded Structure of IF-SPECK

- Without external encoding, the first encoded round function is defined as

$$
\overline{E^{(1)}}=C^{(2)} \circ E^{(1)} \circ A^{(1)}=C^{(2)} \circ\left(B^{(1)}\right)^{-1} \circ E^{(1)} .
$$

- The encoded structure of the first two rounds:

- If $B^{(1)}$ is affine, $\overline{E^{(1)}}$ is encoded by affine encoding.
- If $B^{(1)}$ is quadratic, $\overline{E^{(1)}}$ is encoded by non-linear encoding with unknown (low) degree.


## A Same Structure of SE-SPECK and IF-SEPCK

- By analyzing the round functions of SE-SPECK and IF-SPECK without external encodings, we can obtain a function $F$ which has the same structure as the first two rounds in both two white-box implementations.



## An Encoded Structure of SE-SPECK and IF-SEPCK

- Combining the first three rounds of SE-SPECK and the first two rounds of IF-SPECK:



## An Encoded Structure of SE-SPECK and IF-SEPCK

- The target function of SE-SPECK and IF-SEPCK:

- The collected computation traces consist of $\left(s_{0}, s_{1}\right)$.
- The sensitive values $\left(t_{0}, t_{1}\right)$ are protected by a linear/non-linear encoding $E C$.
- Its construction is irrelevant to the implicit function and the input encoding.


## CA on SE-SPECK and IF-SPECK

- With a key guess $k$ and an input $x$, CA computes a sensitive vector $\left(z_{1}, z_{2}, \cdots, z_{2 n}\right)$.
- CA intends to computes the correlation between $z_{i}$ and $y_{i}$.
- Because of encoding EC, CA needs to enumerate the combination of $\left(z_{1}, z_{2}, \cdots, z_{2 n}\right)$.
encoding $C \circ B^{-1}$ with unknown degree



## Challenges of CA against White-Box ARX

- Large spaces of inputs and key candidates: CA needs to compute the outputs of the modular addition based on the inputs and key guesses.
- Large encoding: CA needs to enumerate the linear combination of the sensitive values to recover the affine encoding. Moreover, it is hard to defeat the quadratic encoding.


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## An Overview of CP-CA

A Chosen-Plaintext Computation Analysis (CP-CA) attack consists of the following three phases:

- Adaptive chosen plaintexts: constructs an adaptive function with a key guess to compute the plaintexts with chosen inputs (principal: a small subset of the full space).
- Correlation computation: invokes the algorithm with the obtained plaintexts and applies the existing computation analysis methods, such as DCA and ADCA to analyze the computation traces.
- Iterative attack: repeats for other key candidates. Distinguishing the correct key based on the ranking method of the corresponding computation analysis.


## Adaptive Function

An adaptive function:

- is applied to choose the plaintexts of the cryptographic algorithm.
- is constructed by some reverse steps of the cryptographic algorithm.
- needs to be instantiated by a key guess.



## Adaptive Function

- The adaptive function $G_{k}$ calculates the plaintexts $\left(x_{0}, x_{1}\right)$ by the inverse of $\left(t_{0}, t_{1}\right)$.

- If key guess $k$ equals to the correct key $k^{*},\left(t_{0}, t_{1}\right)=\left(z_{0}, z_{1}\right)$.
- Otherwise, $\left(t_{0}, t_{1}\right)$ are almost random values.


## (In)Correct Key Guess

If key guess is correct:

- The collected values $\left(s_{0}, s_{1}\right)$ are equal to the outputs of an affine/non-linear function $E C\left(z_{0}, z_{1}\right)$.
- If $E C$ is affine, $\left(s_{0}, s_{1}\right)$ are linear combinations of $\left(z_{0}, z_{1}\right)$.
- If $E C$ is non-linear, $\left(s_{0}, s_{1}\right)$ can be represented by a degree-d ANF of $\left(z_{0}, z_{1}\right)$.
If key guess is incorrect:
equality

$F_{k^{*}}^{\prime}$
- $\left(s_{0}, s_{1}\right)$ are correlated to random $\left(t_{0}, t_{1}\right)$.


## Affine Self-Equivalence

## Theorem

Let $z \in\{0,1\}^{n_{a}}$ denote an $n_{a}$-bit vector, $c$ be an n-bit constant, and $C_{0}$ represent an $\left(n_{b}\left(=n-n_{a}\right)\right)$-bit zero vector. Given an $2 n$-bit affine function $A E: \mathbb{F}_{2}^{2 n} \mapsto \mathbb{F}_{2}^{2 n}$, the resulting vector $A E\left(C_{0} \| z, c\right)$ can also be computed as $L^{\prime} \cdot z \oplus I$, where $L^{\prime}$ is a $2 n \times n_{a}$ matrix and $I \in\{0,1\}^{2 n}$.

- If $E C$ is affine, $\left(s_{0}, s_{1}\right)$ are linear combinations of $z$.
- For SPECK32,

$$
\left(z_{0}, z_{1}\right)=(00000000000000 \| z, 00 f f 00 f f 00 f f 00 f f)
$$

- $\left(s_{0}, s_{1}\right)=E C \cdot\left(z_{0}, z_{1}\right)=A E \cdot(z)$ for some unknown affine function $A E$.


## Quadratic Self-Equivalence

- If $E C$ is quadratic, $\left(s_{0}, s_{1}\right)$ are still linear combinations of $z$.
- Because of these fixed input bits, some variables in the monomials of the ANF representations of EC are constants with degree 0 .
- For an instance of the degree-2 quadratic encoding case, the probability $p$ that a monomial in the ANF has degree 2 is

$$
p=\binom{n_{a}}{2} /\binom{2 n}{2}=\frac{n_{a}\left(n_{a}-1\right)}{2 n(2 n-1)} .
$$

| Block size | 32 | 48 | 64 | 96 | 128 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $p$ | $5.65 \%$ | $2.48 \%$ | $1.39 \%$ | $0.61 \%$ | $0.34 \%$ |

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## CP-DCA

- CP-DCA calculates the correlation between a subset of linear combinations of the chosen inputs and the samples of traces.
- The key guess with the maximum number of the highest correlation is the most likely correct.


## Corollary

Let $y_{i}(1 \leq i \leq 2 n)$ denote the output coordinate of $A E\left(C_{0} \| z, c\right)$. There exist $2 n$ linear combinations $L$ of $z$ satisfying $\left|\operatorname{Cor}\left(L \cdot z, y_{i}\right)\right|=1$.

## CP-DCA Distinguisher

- The CP-DCA distinguisher $\delta_{k}^{\mathrm{CP}-\mathrm{DCA}}$ is defined as follows.

$$
\delta_{k}^{\mathrm{CP}-\mathrm{DCA}}=\arg \max \#\left\{\max \left|\operatorname{Cor}\left(L \cdot z^{(i)},\left(\boldsymbol{v}^{(i)}\right)_{j}\right)\right|\right\}
$$

linear combinations


## Time Complexity of CP-DCA

- Traces collection: $\mathcal{O}(|\mathcal{K}| \cdot N)$ with $|\mathcal{K}| \leftarrow$ key space, $N \leftarrow$ input space.
- Correlation computation: $\mathcal{O}\left(|\mathcal{K}| \cdot 2^{n_{a}} \cdot t \cdot N\right)$ with $2^{n_{a}}$ linear combinations, $t \leftarrow$ the number of trace samples.
- Searching for the highest correlation: $\mathcal{O}\left(|\mathcal{K}| \cdot 2^{n_{a}}\right)$.
- Overall time complexity: $\mathcal{O}\left(|\mathcal{K}| \cdot 2^{n_{a}} \cdot t \cdot N\right)$.


## CP-ADCA

- The degree-1 CP-ADCA constructs a linear system that consists of the coordinates of $x \in \mathcal{X}$ and each sample of $\boldsymbol{v}$.
- The key guess with the maximum number of solvable linear systems is the most likely correct one.


## Corollary

Let $y_{i}(1 \leq i \leq 2 n)$ denote the output coordinate of $A E\left(C_{0} \| z, c\right)$. Let $Z_{j}\left(1 \leq j \leq n_{a}\right)$ denote the bits of $z$. There exist $2 n$ vectors $a=\left(a_{0}, a_{1}, \cdots, a_{n_{a}}\right)$ satisfying

$$
\left[\begin{array}{llll}
1 & Z_{1} & \cdots & Z_{n_{\mathrm{a}}}
\end{array}\right] \cdot a^{T}=y_{i}, \text { for } 1 \leq i \leq 2 n .
$$

## CP-ADCA Distinguisher

- The CP-ADCA distinguisher $\delta_{k}^{\mathrm{CP}-\mathrm{ADCA}}$ is defined as follows.

$$
\delta_{k}^{\text {CP-ADCA }}=\arg \max \#\left\{r(Z) \geq r\left(Z \mid v_{i}\right)\right\}
$$



## Time Complexity of ADCA

- Traces collection: $\mathcal{O}(|\mathcal{K}| \cdot N)$ with $|\mathcal{K}| \leftarrow$ key space, $N \leftarrow$ input space.
- Computation of linear systems: $\mathcal{O}\left(|\mathcal{K}| \cdot t \cdot N \cdot\left(n_{a}+1\right)\right)$ with the steps for calculating $r\left(Z \mid v_{i}\right)$ are $N \cdot\left(n_{a}+1\right), t \leftarrow$ the number of trace samples.
- Searching for the maximum number of solvable linear systems: $\mathcal{O}(|\mathcal{K}|)$.
- Overall time complexity: $\mathcal{O}\left(|\mathcal{K}| \cdot t \cdot N \cdot\left(n_{a}+1\right)\right)$.


## Parameters of CP-DCA and CP-ADCA

- CP-CA can be instantiated with different parameters, such as the chosen input space $n_{a}$, the constant input $c$, the number of traces $N$, the number of trace samples $t$.

| Block size | $n_{b}$ | $n_{a}$ | c | $N$ | $t$ | Time complexity |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | CP-DCA | CP-ADCA | DCA | AC |
| 32 | 8 | 8 | 00ff | 256 | 32 | $2^{37}$ | $2^{31.32}$ | $2^{69}$ | $2^{30} \sim 2^{45}$ |
| 48 | 16 |  | ff00ff |  | 48 | $2^{45.58}$ | $2^{39.90}$ | $2^{101.58}$ | $2^{33} \sim 2^{50}$ |
| 64 | 24 |  | OOff00ff |  | 64 | $2^{54}$ | $2^{48.32}$ | $2^{134}$ | $2^{36} \sim 2^{54}$ |
| 96 | 40 |  | 00ff00ff00ff |  | 96 | $2^{70.58}$ | $2^{64.90}$ | $2^{198.58}$ | $2^{39} \sim 2^{59}$ |
| 128 | 56 |  | OOff00ff00ff00ff |  | 128 | $2^{87}$ | $2^{81.32}$ | $2^{263}$ | $2^{42} \sim 2^{63}$ |

## Simulations

- Performing the simulations of CP-DCA and CP-ADCA against the 32-bit encoded structure with affine output encodings.
- CP-DCA and CP-ADCA can successfully recover the secret key for the 32-bit block size.

| Attack | Block | Key guess |  | Count of recovered |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | size | Range | Count | Key | Encoding |
| CP-DCA | 32 | $0000-\mathrm{ffff}$ | $2^{16}$ | 1 | 32 |
| CP-ADCA |  |  |  |  |  |

## SE-SPECK and IF-SPECK implementations

- Implement SE-SPECK and IF-SPECK with block sizes 32 and 48 thorough the open-source scripts.
- Intel Core $\mathbf{i} 7-11800 \mathrm{H}$ processor $@ 2.30 \mathrm{GHz}$ and 40GB RAM.

| Cipher | Encoding | Degree | Source Code <br> size (MB) | Binary size <br> $(\mathrm{MB})$ | RAM <br> $(\mathrm{MB})$ | Execution <br> time (ms) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SE32/K64 | affine | - | 0.08 | 0.04 | 1.11 | 0.06 |
| SE48/K96 | affine | - | 0.18 | 0.07 | 1.17 | 0.14 |
| IF32/K64 | affine | 2 | 0.16 | 0.15 | 3.08 | 2.43 |
|  | quadratic | 2 | 0.16 | 0.15 | 3.15 | 2.46 |
|  |  | 3 | 1.85 | 1.82 | 5.30 | 11.63 |
|  |  | 4 | 17.45 | 17.41 | 24.43 | 83.33 |

## Practical attacks of CP-DCA and CP-ADCA

- CP-DCA and CP-ADCA can successfully distinguish the secret key over the full key space.

| Cipher | Encoding | Degree | CP-DCA |  | CP-ADCA |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Count of | recov |  |
|  |  |  | Key | Encoding | Key | Encoding |
| SE32/K64 | affine | - | 1 | 18 | 1 | 19 |
| SE48/K96 | affine | - |  | 25 |  | 36 |
| IF32/K64 | affine | 2 |  | 32 |  | 32 |
|  | quadratic | 2 |  |  |  |  |
|  |  | 3 |  |  |  |  |
|  |  | 4 |  |  |  |  |

## Compare with Chosen-Plaintext SCA

CP-CA:

- constructs an adaptive function $\rightarrow$ computes the target plaintexts.

Adaptive Side-Channel Analysis (ASCA):

- analyzes the side-channel information $\rightarrow$ choose the target plaintexts.



## Possible Countermeasure of CP-CA

- The quadratic non-linear encoding can be bypassed by the adaptive function of the first-degree CP-CA.
- The possible countermeasure is to apply higher-degree non-linear encoding.

The open problems:

- The method to generate the higher-degree self-equivalences of modular addition?
- The resistance of higher-degree non-linear encoding against higher-degree CP-CA?


## Possible Improvement of CP-CA

- The most optimal choice for the parameters of ACP-DCA.
- The vector space of linear combinations,
- the number of required traces,
- and the constant inputs.
- Small key space. It costs a higher time complexity in the large block size cases.
- A specific analysis dedicated to the sparse affine self-equivalences.


## Outline

## 1. ARX-Based White-Box Ciphers

2. Computation Analysis against White-Box SPECK
3. Chosen-Plaintext Computation Analysis
4. Attack Instances of CP-DCA and CP-ADCA
5. Conclusion

## Conclusion

- The large spaces of inputs, key candidates, and encodings of ARX-based white-box ciphers can prevent a practical DCA attack.
- CP-CA attacks exploit the chosen plaintexts phase to reduce the large affine encoding into small linear one.
- The adaptive function can bypass the quadratic self-equivalence of IF-SPECK.
- SE-SPECK and IF-SPECK are vulnerable to CP-CA attacks.


## Thanks for your attention!

